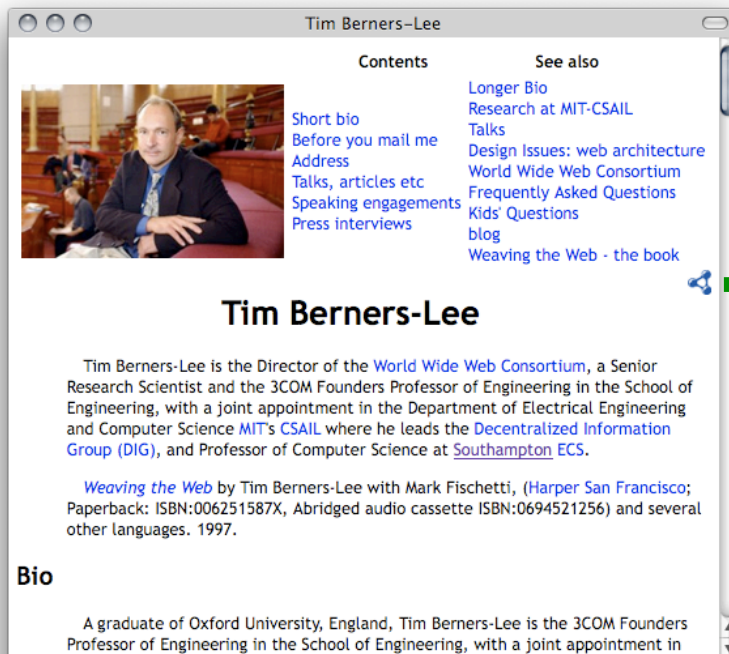


Unit 4: SPARQL1.0 in Detail & SPARQL's formal semantics

Recall from Lecture 1/Assignment 1

Lots of RDF data already published, e.g. about **Tim Berners-Lee**

FOAF/RDF linked from a home page: personal data (foaf:name, foaf:phone, etc.), relationships foaf:knows, rdfs:seeAlso)



```

Source of: http://www.w3.org/People/Berners-Lee/card#i
<!-- Processed by Id: cwm.py,v 1.197 2007/12/13 15:38:39 syosi Exp -->
<!-- using base file:///devel/WWW/People/Berners-Lee/card.n3-->

<rdf:RDF xmlns="http://xmlns.com/foaf/0.1/"
  xmlns:cc="http://creativecommons.org/ns#"
  xmlns:con="http://www.w3.org/2000/10/swap/pim/contact#"
  xmlns:dc="http://purl.org/dc/elements/1.1/"
  xmlns:foaf="http://xmlns.com/foaf/0.1/"
  xmlns:geo="http://www.w3.org/2003/01/geo/wgs84_pos#"
  xmlns:owl="http://www.w3.org/2002/07/owl#"
  xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
  xmlns:s="http://www.w3.org/2000/01/rdf-schema#">

  <rdf:Description rdf:about="http://www.w3.org/2002/01/tr-automation/tr.rdf">
    <dc:title>W3C Standards and Technical Reports</dc:title>
  </rdf:Description>

  <PersonalProfileDocument rdf:about="">
    <cc:license rdf:resource="http://creativecommons.org/licenses/by-nc/3.0/" />
    <dc:title>Tim Berners-Lee's FOAF file</dc:title>
    <maker rdf:resource="http://www.w3.org/People/Berners-Lee/card#i" />
    <primaryTopic rdf:resource="http://www.w3.org/People/Berners-Lee/card#i" />
  </PersonalProfileDocument>

```

Recall from Lecture 1/Assignment 1

Also from exports ... if they're up and running (sorry about that)

The image shows two browser windows. The left window displays the DBLP website for Tim Berners-Lee, including a list of publications from 2008. The right window shows the RDF export of the same page, listing properties and their values (URIs).

Property	Value
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/conf/aaai/KagalBCW06>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/conf/policy/HansonBKS07>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/conf/policy/KagalBCW06>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/conf/sigopsE/Berners-Lee88>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/conf/w3c/Berners-LeeCPS05>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/conf/www/Berners-Lee05>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/conf/www/BizerHIB08>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/conf/www/ShadboltBH06>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/journals/cacm/Berners-Lee97>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/journals/cacm/Berners-LeeCLNS94>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/journals/cacm/HendlerSHB08>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/journals/cacm/WeitznABFHS08>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/journals/cn/Berners-LeeCG92>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/journals/computer/Berners-Lee96>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/journals/corr/abs-0711-1533>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/journals/en/Berners-LeeCGP92>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/journals/expert/ShadboltBH06>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/journals/tweb/Berners-LeeHHOSW06>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/journals/tlp/Berners-LeeCKSH08>
is dc:creator of	<http://dblp.l3s.de/d2r/resource/publications/www/org/w3/http1-1>

Gives unique URIs to authors, documents, etc. on DBLP! E.g.,

http://dblp.l3s.de/d2r/resource/authors/Tim_Berners-Lee,

<http://dblp.l3s.de/d2r/resource/publications/journals/tlp/Berners-LeeCKSH08>

Provides RDF version of all DBLP data and even a SPARQL query interface!

RDF Data at http://dblp.l3s.de/d2r/resource/authors/Tim_Berners-Lee



Property	Value
is dc:creator of	< http://dblp.l3s.de/d2r/resource/publications/conf/aaai/KagalBCW06 >
is dc:creator of	< http://dblp.l3s.de/d2r/resource/publications/conf/chi/schraefelAWTBCJKDMMSSW09 >
is dc:creator of	< http://dblp.l3s.de/d2r/resource/publications/conf/esws/OmitolaKPYSSBGHsS10 >
is dc:creator of	< http://dblp.l3s.de/d2r/resource/publications/conf/policy/HansonBKS07 >
is dc:creator of	< http://dblp.l3s.de/d2r/resource/publications/conf/policy/KagalBCW06 >
...	...
foaf:homepage	< http://www.w3.org/People/Berners-Lee/ >
rdfs:label	Tim Berners-Lee
is foaf:maker of	< http://dblp.l3s.de/d2r/resource/publications/conf/aaai/KagalBCW06 >
is foaf:maker of	< http://dblp.l3s.de/d2r/resource/publications/conf/chi/schraefelAWTBCJKDMMSSW09 >
is foaf:maker of	< http://dblp.l3s.de/d2r/resource/publications/conf/esws/OmitolaKPYSSBGHsS10 >
is foaf:maker of	< http://dblp.l3s.de/d2r/resource/publications/conf/policy/HansonBKS07 >
is foaf:maker of	< http://dblp.l3s.de/d2r/resource/publications/conf/policy/KagalBCW06 >
...	...
foaf:name	Tim Berners-Lee
rdfs:seeAlso	< http://dblp.l3s.de/Authors/Tim+Berners-Lee >
rdfs:seeAlso	< http://www.bibsonomy.org/uri/author/Tim+Berners-Lee >
rdf:type	foaf:Agent

http://dblp.l3s.de/d2r/resource/publications/conf/esws/OmitolaKPYSSBGHsS10

Tor Disabled

We know how this data looks in Turtle syntax...

- DBLP Data in RDF: Triples Turtle Syntax:

```
@prefix rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>.
```

```
@prefix dcterms: <http://purl.org/dc/terms/> .
```

```
@prefix foaf: <http://xmlns.com/foaf/0.1/> .
```

```
@prefix xsd: <http://www.w3.org/2001/XMLSchema#> .
```

```
@prefix swrc: <http://swrc.ontoware.org/ontology#> .
```

```
<http://dblp.13s.../journals/tplp/Berners-LeeCKSH08> rdf:type swrc:Article.
```

```
<http://dblp.13s.../journals/tplp/Berners-LeeCKSH08> dcterms:issued "2008"^^xsd:gYear .
```

```
<http://dblp.13s.../journals/tplp/Berners-LeeCKSH08> foaf:maker <http://dblp.13s.../Tim_Berners-Lee> .
```

```
<http://dblp.13s.../journals/tplp/Berners-LeeCKSH08> foaf:maker <http://dblp.13s.../Dan_Connolly> .
```

```
<http://dblp.13s.../journals/tplp/Berners-LeeCKSH08> foaf:maker <http://dblp.13s.../Jim_Hendler> .
```

```
<http://dblp.13s.../journals/tplp/Berners-LeeCKSH08> foaf:maker <http://dblp.13s.../Lalana_Kagal> .
```

```
<http://dblp.13s.../journals/tplp/Berners-LeeCKSH08> foaf:maker <http://dblp.13s.../Yosi_Scharf> .
```

...

```
<http://dblp.13s.../conf/aaai/KagalBCW06> rdf:type swrc:inProceedings .
```

```
<http://dblp.13s.../conf/aaai/KagalBCW06> foaf:maker <http://dblp.13s.../Tim_Berners-Lee> .
```

...

```
<http://dblp.13s.../Tim_Berners-Lee> foaf:homepage <http://www.w3.org/People/Berners-Lee/> .
```

```
<http://dblp.13s.../Tim_Berners-Lee> foaf:name "Tim Berners-Lee" .
```

We know how the shortcuts of Turtle syntax...

- DBLP Data in RDF: Triples Turtle Syntax:

```
@prefix rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>.
```

```
@prefix dcterms: <http://purl.org/dc/terms/> .
```

```
@prefix foaf: <http://xmlns.com/foaf/0.1/> .
```

```
@prefix xsd: <http://www.w3.org/2001/XMLSchema#> .
```

```
@prefix swrc: <http://swrc.ontoware.org/ontology#> .
```

```
<http://dblp.13s.../journals/tplp/Berners-LeeCKSH08> rdf:type swrc:Article ;
dcterms:issued "2008"^^xsd:gYear ;
foaf:maker <http://dblp.13s.../Tim_Berners-Lee> ,
          <http://dblp.13s.../Dan_Connolly> ,
          <http://dblp.13s.../Jim_Hendler> ,
          <http://dblp.13s.../Lalana_Kagal> ,
          <http://dblp.13s.../Yosi_Scharf> .
```

...

```
<http://dblp.13s.../conf/aaai/KagalBCW06> rdf:type swrc:inProceedings ;
foaf:maker <http://dblp.13s.../Tim_Berners-Lee> .
```

...

```
<http://dblp.13s.../Tim_Berners-Lee> foaf:homepage <http://www.w3.org/People/Berners-Lee/> ;
foaf:name "Tim Berners-Lee" .
```

SPARQL 1.0 in Detail:

Let's focus on SELECT queries first...

In more detail than in lecture 1:

- Basic Graph Patterns
- UNION patterns
- OPTIONAL Patterns
- FILTERs
- GRAPH graph patterns & Datasets
- ORDER BY / LIMIT / OFFSET

Basic Graph Patterns

A **triple pattern** is an RDF triple, optionally containing variables (prefixed by '?') in either s/p/o position.

A **basic graph pattern** is a set of triple patterns.

Informally, SPARQL tries to match these patterns against a given RDF graph and returns as solution ***multi-sets of possible bindings*** for the variables in the pattern.

Example: Basic graph pattern matching

```
{ ?D foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee> .
    ?D foaf:maker ?CoAuth .
    ?CoAuth foaf:name ?N }
```

```
<http://dblp.13s.../journals/tplp/Berners-LeeCKSH08> rdf:type swrc:Article ;
                                                    dcterms:issued "2008"^^xsd:gYear ;
                                                    foaf:maker <http://dblp.13s.../Tim_Berners-Lee> ,
                                                    <http://dblp.13s.../Dan_Connolly> ,
                                                    <http://dblp.13s.../Jim_Hendler> ,
                                                    <http://dblp.13s.../Lalana_Kagal> ,
                                                    <http://dblp.13s.../Yosi_Scharf> .
```

```
<http://dblp.13s.../Tim_Berners-Lee> foaf:homepage <http://www.w3.org/People/Berners-Lee/> ;
                                       foaf:name "Tim Berners-Lee" .
```

```
<http://dblp.13s.../Dan_Connolly> foaf:name "Dan Connolly" .
<http://dblp.13s.../Jim_Hendler> foaf:name "James Hendler" .
<http://dblp.13s.../Lalana_Kagal> foaf:name "Lalana Kagal" .
<http://dblp.13s.../Yosi_Scharf> foaf:name "Yosi Scharf" .
```

Example: Basic graph pattern matching

```
{ ?D foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee> .
    ?D foaf:maker ?CoAuth .
    ?CoAuth foaf:name ?N }
```

```
<http://dblp.13s.../journals/tp1p/Berners-LeeCKSH08> rdf:type swrc:Article ;
    dcterms:issued "2008"^^xsd:gYear ;
    foaf:maker <http://dblp.13s.../Tim_Berners-Lee> ,
    <http://dblp.13s.../Dan_Connolly> ,
    <http://dblp.13s.../Jim_Hendler> ,
    <http://dblp.13s.../Lalana_Kagal> ,
    <http://dblp.13s.../Yosi_Scharf> .
```

```
<http://dblp.13s.../Tim_Berners-Lee> foaf:homepage <http://www.w3.org/People/Berners-Lee/> ;
    foaf:name "Tim Berners-Lee" .
```

```
<http://dblp.13s.../Dan_Connolly> foaf:name "Dan Connolly" .
<http://dblp.13s.../Jim_Hendler> foaf:name "James Hendler" .
<http://dblp.13s.../Lalana_Kagal> foaf:name "Lalana Kagal" .
<http://dblp.13s.../Yosi_Scharf> foaf:name "Yosi Scharf" .
```

Example: Basic graph pattern matching

```
{ ?D foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee> .
    ?D foaf:maker ?CoAuth .
    ?CoAuth foaf:name ?N }
```

```
<http://dblp.13s.../journals/tplp/Berners-LeeCKSH08> rdf:type swrc:Article ;
    dcterms:issued "2008"^^xsd:gYear ;
    foaf:maker <http://dblp.13s.../Tim_Berners-Lee> ,
               <http://dblp.13s.../Dan_Connolly> ,
               <http://dblp.13s.../Jim_Hendler> ,
               <http://dblp.13s.../Lalana_Kagal> ,
               <http://dblp.13s.../Yosi_Scharf> .
```

```
<http://dblp.13s.../Tim_Berners-Lee> foaf:homepage <http://www.w3.org/People/Berners-Lee/> ;
    foaf:name "Tim Berners-Lee" .
```

```
<http://dblp.13s.../Dan_Connolly> foaf:name "Dan Connolly" .
<http://dblp.13s.../Jim_Hendler> foaf:name "James Hendler" .
<http://dblp.13s.../Lalana_Kagal> foaf:name "Lalana Kagal" .
<http://dblp.13s.../Yosi_Scharf> foaf:name "Yosi Scharf" .
```

Example: Basic graph pattern matching

```
{ ?D foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee> .
  ?D foaf:maker ?CoAuth .
  ?CoAuth foaf:name ?N }
```

?D	?CoAuth	?N
Berners-LeeCKSH0	:Tim_Berners-Lee	"Tim Berners-Lee"
Berners-LeeCKSH0	:Dan_Connolly	"Dan Connolly"
Berners-LeeCKSH0	:Jim_Hendler	"James Hendler"
Berners-LeeCKSH0	:Lalana_Kagal	"Lalana Kagal"
Berners-LeeCKSH0	:Yosi_Scharf	"Yosi Scharf"

Example: Basic graph pattern matching

```
{ ?D foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee> .
    ?D foaf:maker ?CoAuth .
    ?CoAuth foaf:name ?N }
```

Solution =

```
{ {?D → Berners-LeeCKSH0, ?CoAuth → :Tim_Berners-Lee, ?N → "Tim Berners-Lee" } ,
  {?D → Berners-LeeCKSH0, ?CoAuth → :Dan_Connolly , ?N → "Dan Connolly" } ,
  {?D → Berners-LeeCKSH0, ?CoAuth → :Jim_Hendler , ?N → "James Hendler" } ,
  {?D → Berners-LeeCKSH0, ?CoAuth → :Lalana_Kagal , ?N → "Lalana Kagal" } ,
  {?D → Berners-LeeCKSH0, ?CoAuth → :Yosi_Scharf , ?N → "Yosi Scharf" } }
```

Example: Basic graph pattern matching

```
{<http://dblp.13s.../journals/tplp/Berners-LeeCKSH08> foaf:maker  
<http://dblp.13s.de/.../authors/Tim_Berners-Lee>. }
```

Solution =

$\{\emptyset\}$

Matches, with one
empty binding.

Note: $\{\}$ \neq $\{\emptyset\}$

Example: Basic graph pattern matching

```
{<http://dblp.13s.../journals/tplp/Berners-LeeCKSH08> foaf:maker  
<http://dblp.13s.de/.../authors/Thomas Eiter>. }
```

Solution =

{ }

Doesn't match
anything.

Note: $\{\}$ \neq $\{\emptyset\}$

SELECT (DISTINCT) & ASK

“Result forms” SELECT & ASK are defined on top of pattern matching:

- SELECT ... Projection
- ASK ... True/False, i.e. (returns **Solution != {}**)

SELECT (DISTINCT) & ASK

“Result forms” SELECT & ASK are defined on top of pattern matching:

- SELECT ... Projection

```
SELECT *
WHERE { ?D foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee>.
       ?D foaf:maker ?CoAuth .
       ?CoAuth foaf:name ?N }

```

Solution =

```
{ {?D → Berners-LeeCKSH0, ?CoAuth → :Tim_Berners-Lee, ?N → "Tim Berners-Lee" } ,
  {?D → Berners-LeeCKSH0, ?CoAuth → :Dan_Connolly , ?N → "Dan Connolly" } ,
  {?D → Berners-LeeCKSH0, ?CoAuth → :Jim_Hendler , ?N → "James Hendler" } ,
  {?D → Berners-LeeCKSH0, ?CoAuth → :Lalana_Kagal , ?N → "Lalana Kagal" } ,
  {?D → Berners-LeeCKSH0, ?CoAuth → :Yosi_Scharf , ?N → "Yosi Scharf" } }

```

SELECT (DISTINCT) & ASK

“Result forms” SELECT & ASK are defined on top of pattern matching:

- SELECT ... Projection

```
SELECT ?D
WHERE {
  ?D foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee>.
  ?D foaf:maker ?CoAuth .
  ?CoAuth foaf:name ?N }

```

Solution =

```
{ {?D → Berners-LeeCKSH0 } ,
  {?D → Berners-LeeCKSH0} ,
  {?D → Berners-LeeCKSH0} ,
  {?D → Berners-LeeCKSH0} ,
  {?D → Berners-LeeCKSH0 } }

```

SELECT (DISTINCT) & ASK

“Result forms” SELECT & ASK are defined on top of pattern matching:

- SELECT **DISTINCT** ... Projection+eliminate duplicates

```
SELECT DISTINCT ?D
WHERE { ?D foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee>.
       ?D foaf:maker ?CoAuth .
       ?CoAuth foaf:name ?N } }
```

Solution =

{{?D → Berners-LeeCKSH0 } }

SELECT (DISTINCT) & ASK

“Result forms” SELECT & ASK are defined on top of pattern matching:

- SELECT ... Projection to non-occurring variables yields empty binding set

```
SELECT ?X
WHERE { ?D foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee>.
        ?D foaf:maker ?CoAuth .
        ?CoAuth foaf:name ?N }
```

Solution =

{ \emptyset ,
 \emptyset ,
 \emptyset ,
 \emptyset ,
 \emptyset }

SELECT (DISTINCT) & ASK

“Result forms” SELECT & ASK are defined on top of pattern matching:

- **ASK** ... True/False, i.e. (returns **Solution == {}**)

ASK

```
WHERE { ?D foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee> .  
        ?D foaf:maker ?CoAuth .  
        ?CoAuth foaf:name ?N }
```

TRUE

UNIONS of conjunctive queries...

Example:

*“Give me all names of co-authors **or** friends of Tim Berners-Lee”*

```
PREFIX foaf: <http://xmlns.com/foaf/0.1/>
SELECT ?N
WHERE {

```

?N
"Lalana Kagal"
"Tim Berners-Lee"
"Dan Connolly"
"Jim Hendler"
...

U

?N
"Michael Hausenblas"
"Jim Hendler"
"Charles McCathieNevile"
...

=

?N
"Lalana Kagal"
"Tim Berners-Lee"
"Dan Connolly"
"Jim Hendler"
...
"Michael Hausenblas"
"Jim Hendler"
"Charles McCathieNevile"
...

Note: Again: Duplicates Possible by UNION, bag/multiset semantics!

UNIONS of conjunctive queries...

Example:

“Give me all names of co-authors **or** friends of Tim Berners-Lee”

```

PREFIX foaf: <http://xmlns.com/foaf/0.1/>
SELECT ?CoAuthN ?FrN
WHERE {
  { [ foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee>,
    [ foaf:name ?CoAuthN ] ] . }

  UNION

  { <http://www.w3.org/People/Berners-Lee/card#i> foaf:knows ?F .
    ?F foaf:name ?FrN }
}

```

Note: variables can be unbound in a result!

?CoAuthN	?FrN
"Lalana Kagal"	
"Tim Berners-Lee"	
"Dan Connolly"	
"Jim Hendler"	
...	
	"Michael Hausenblas"
	"Jim Hendler"
	"Charles McCathieNevile"
	...

OPTIONAL query parts







Optional parts in queries (Left Outer Join)

Example:

*“Give me all names of co-authors of Tim Berners-Lee and **optionally** their homepage”*

```
PREFIX foaf: <http://xmlns.com/foaf/0.1/>
SELECT ?N ?H
WHERE {
  ?D foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee>.
  ?D foaf:maker ?CoAuth .
  ?CoAuth foaf:name ?N .
  OPTIONAL { ?CoAuth foaf:homepage ?H }
}
```

Another example where variables can be unbound in results!

N	H
"Lalana Kagal"	-
"Tim Berners-Lee"	< http://www.w3.org/People/Berners-Lee/ > 
"Dan Connolly"	-
"Daniel J. Weitzner"	< http://www.w3.org/People/Weitzner.html > 
"m. c. schraefel"	< http://www.ecs.soton.ac.uk/~mc/ > 
"Paul André"	-
"Ryen White"	< http://www.dcs.gla.ac.uk/~whiter/ > 
"Desney S. Tan"	< http://research.microsoft.com/%7Edesney/ > 
"Tim Berners-Lee"	< http://www.w3.org/People/Berners-Lee/ > 
"Sunny Consolvo"	-

FILTERING out query results

FILTERs allow to specify **FILTER** conditions on patterns

Example:

*“Give me all names of co-authors of Tim Berners-Lee and whose homepage starts with **http://www.w3.. different from Tim B.-L. himself**”*

```

PREFIX foaf: <http://xmlns.com/foaf/0.1/>
SELECT ?N ?H
WHERE {
  ?D foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee>.
  ?D foaf:maker ?CoAuth .
  ?CoAuth foaf:name ?N .
  ?CoAuth foaf:homepage ?H .
  FILTER( regex( str(?H) , "^http://www.w3" ) &&
  ?CoAuth != <http://dblp.13s.de/.../authors/Tim_Berners-Lee> )
}

```

N	H
"Daniel J. Weitzner"	<http://www.w3.org/People/Weitzner.html> 
"Daniel J. Weitzner"	<http://www.w3.org/People/Weitzner.html> 
"Daniel J. Weitzner"	<http://www.w3.org/People/Weitzner.html> 
"Daniel J. Weitzner"	<http://www.w3.org/People/Weitzner.html> 
"Daniel J. Weitzner"	<http://www.w3.org/People/Weitzner.html> 
"Daniel J. Weitzner"	<http://www.w3.org/People/Weitzner.html> 

SIEMENS

FILTERING out query results

FILTERs allow to specify FILTER conditions on pattern

- Can use an extensible library of built-in functions
 - checking:** bound(), isIRI(), isBlank(), regex() ...
 - Conversion/extraction:** str(), datatype(), lang() ...
- Can be complex: && , ||, !
- ATTENTION:** Evaluated in a 3-valued logic: **true, false, error**

A	B	A B	A && B
T	T	T	T
T	F	T	F
F	T	T	F
F	F	F	F
T	E	T	E
E	T	T	E
F	E	E	F
E	F	E	F
E	E	E	E

Example FILTERs and OPTIONAL:

```

PREFIX foaf: <http://xmlns.com/foaf/0.1/>
SELECT ?N ?H
WHERE {
    ?D foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee>.
    ?D foaf:maker ?CoAuth . ?CoAuth foaf:name ?N .
    OPTIONAL { ?CoAuth foaf:homepage ?H . }
    FILTER( ! regex( str(?H) , "^http://www.w3" ) &&
    ?CoAuth != <http://dblp.13s.de/.../authors/Tim_Berners-Lee> )
}
    
```

A	!A
T	F
F	T
E	E

N	H
"m. c. schraefel"	<http://www.ecs.soton.ac.uk/~mc/>
"... White"	<http://www.dcs.gla.ac.uk/~whiter/>
"... S. Tan"	<http://research.microsoft.com/%7Edesney/>
"Isaac S. Kohane"	<http://chip.org/~zak/>

Will result in **E** for unbound ?H
 → Whole FILTER expr
 always **E** for unbound ?H
 You don't get those without homepage

FILTERING out query results

- **ATTENTION:** FILTERs can **NOT** assign/create new values...

```
PREFIX ex: <http://example.org/>
```

```
SELECT ?Item ?NewP
```

```
WHERE { ?Item ex:price ?Pr FILTER (?NewP = ?Pr + 10 ) }
```

New "Non-safe" variable in FILTERs are considered unbound. The Filter will just always result in **E**
→ Result always empty

- Obviously, common query languages like SQL can do this...

```
SELECT Item, Price+10 AS NewPrice FROM Table
```

... FILTER in SPARQL is like WHERE in SQL,
but SPARQL1.0 doesn't have assignment (AS)

Querying named GRAPHS 1/2

*Find me people who have been involved with **at least three** ISWC or ESWC conference events.*

(from SPARQL endpoint at data.semanticweb.org)

```
SELECT ?person WHERE {  
  GRAPH ?g1 { ?person a foaf:Person }  
  GRAPH ?g2 { ?person a foaf:Person }  
  GRAPH ?g3 { ?person a foaf:Person }  
  FILTER(?g1 != ?g2 && ?g1 != ?g3 && ?g2 != ?g3) . }
```

The GRAPH ?g construct allows a pattern to match against one of the named graphs in the **RDF dataset**. The URI of the matching graph is bound to ?g (or whatever variable was actually used). The FILTER assures that we're finding a person who occurs in three *distinct* graphs.

Querying named GRAPHS 1/2

An RDF dataset is a set $D = \{G, (G_1, N_1), \dots (G_n, N_n)\}$ consisting of

- The **default graph** G
- **Named graphs**, i.e. pairs of Graphs and Names (G_n, N_n)

The RDF dataset of a query can be

- Implicitly given (like in the query on the last slide)
- Explicitly specified by **FROM**, **FROM NAMED** clauses

(explicit specification of the dataset may be forbidden in case the dataset is fixed implicitly)

```
SELECT ?person
FROM <http://polleres.net/foaf.rdf>
FROM <http://gibbi.com/foaf.rdf>
WHERE {
    ?person a foaf:Person
}
```

$DS = \{D\}$ such that $D = G_{\text{polleres.net}} \cup G_{\text{gibbi.com}}$

If given explicitly via FROM/FROM NAMED clauses the default graph of the Dataset is the RDF merge of the graphs given in FROM clauses

Querying named GRAPHS 1/2

An RDF dataset is a set $D = \{G, (G_1, N_1), \dots (G_n, N_n)\}$ consisting of

- The **default graph** G
- **Named graphs**, i.e. pairs of Graphs and Names (G_n, N_n)

The RDF dataset of a query can be

- Implicitly given (like in the query on the last slide)
- Explicitly specified by **FROM**, **FROM NAMED** clauses

(explicit specification of the dataset may be forbidden in case the dataset is fixed implicitly)

```
SELECT ?G ?person
FROM NAMED <http://polleres.net/foaf.rdf>
FROM NAMED <http://gibbi.com/foaf.rdf>
WHERE {
    GRAPH ?G { ?person a foaf:Person }
}
```

$D = \{G, (G_{\text{polleres.net}}, \text{http://polleres.net/foaf.rdf}), (G_{\text{gibbi.com}}, \text{http://gibbi.com/foaf.rdf})\}$
 such that $G = \{ \}$

Querying named GRAPHS 1/2

An RDF dataset is a set $DS = \{D, (G_1, N_1), \dots (G_n, N_n)\}$ consisting of

- The **default graph** D
- **Named graphs**, i.e. pairs of Graphs and Names (G_n, N_n)

The RDF dataset of a query can be

- Implicitly given (like in the query on the last slide)
- Explicitly specified by **FROM**, **FROM NAMED** clauses

(explicit specification of the dataset may be forbidden in case the dataset is fixed implicitly)

```
SELECT ?G ?person
FROM NAMED <http://polleres.net/foaf.rdf>
FROM NAMED <http://gibbi.com/foaf.rdf>
WHERE {
    { ?person a foaf:Person }
}
```

Note: No results, since
Default Graph is empty.

$DS = \{G, (G_{\text{polleres.net}}, \text{http://polleres.net/foaf.rdf}), (G_{\text{gibbi.com}}, \text{http://gibbi.com/foaf.rdf})\}$
such that $G = \{\}$

Querying named GRAPHS 1/2

An RDF dataset is a set $D = \{G, (G_1, N_1), \dots, (G_n, N_n)\}$ consisting of

- The **default graph** G
- **Named graphs**, i.e. pairs of Graphs and Names (G_n, N_n)

The RDF dataset of a query can be

- Implicitly given (like in the query on the last slide)
- Explicitly specified by **FROM**, **FROM NAMED** clauses

(explicit specification of the dataset may be forbidden in case the dataset is fixed implicitly)

```
SELECT ?G ?person
FROM NAMED <http://polleres.net/foaf.rdf>
FROM NAMED <http://gibbi.com/foaf.rdf>
WHERE {
  GRAPH <http://www.w3.org/timbl/Card> { ?person a foaf:Person }
}
```

Note: No results, since there is no graph named <http://w3.org/timbl/Card> in the dataset

$D = \{G, (G_{\text{polleres.net}}, \text{http://polleres.net/foaf.rdf}), (G_{\text{gibbi.com}}, \text{http://gibbi.com/foaf.rdf})\}$
 such that $G = \{\}$

Slicing and Dicing results

Solution Modifiers

- ORDER BY
- LIMIT/OFFSET

Example:

```
SELECT ?P
FROM <G>
WHERE { ?P foaf:Person }
ORDER BY ?P
LIMIT 5
```

Graph G:

```
:p1 a foaf:Person.
:p2 a foaf:Person.
...
:p100 a foaf:Person.
```

?P
:p1
:p2
:p3
:p4
:p5

Slicing and Dicing results

Solution Modifiers

- ORDER BY
- LIMIT/OFFSET

Example:

```
SELECT ?P
FROM <G>
WHERE { ?P foaf:Person }
ORDER BY ?P
LIMIT 5
OFFSET 5
```

Graph G:

```
:p1 a foaf:Person.
:p2 a foaf:Person.
...
:p100 a foaf:Person.
```

?P
:p6
:p7
:p8
:p9
:p10

Slicing and Dicing results

Solution Modifiers

- ORDER BY
- LIMIT/OFFSET

Example:

```
SELECT ?P
FROM <G>
WHERE { ?P foaf:Person }
```

```
LIMIT 5
OFFSET 5
```

Graph G:

```
:p1 a foaf:Person.
:p2 a foaf:Person.
...
:p100 a foaf:Person.
```

ATTENTION! Order is Important when LIMIT and OFFSET are used to achieve deterministic results!

?P
:p8
:p2
:p99
:p20
:p42

More complex query examples 1/2

“IF-THEN-ELSE”

- *“Give me the names of persons, if it exists, otherwise the nicknames, if it exists, otherwise the labels”*

```

SELECT ?X ?N
WHERE {
  ?X { rdfs:type foaf:Person
    OPTIONAL { ?X foaf:name ?N } }
  OPTIONAL { ?X foaf:nickname ?N } }
  OPTIONAL { ?X rdfs:label ?N } }

```

OPTIONAL is
order-dependent!
OPTIONAL is NOT
modular/compositional!
(?N is not considered
unsafe in this FILTER)*

“Conditional OPTIONAL”

- *“Give me the names, and the homepage only of those whose name starts with ‘D’”*

```

SELECT ?N ?H
WHERE {
  ?X foaf:name ?N
    OPTIONAL { ?X foaf:homepage ?H
      FILTER ( regex ( str(?N), "^D" ) ) }
}

```

More complex query examples 2/2

Negation is doable in SPARQL1.0:

- *“Give me all Persons without a homepage”*
- **Option 1:** by combination of OPTIONAL and FILTER(!bound(...))

```
SELECT ?X
WHERE{ ?X rdf:type foaf:Person
       OPTIONAL { ?X foaf:homepage ?H }
       FILTER( !bound( ?H ) ) }
```

- **Option 2:** by another weird combination of OPTIONAL with GRAPH queries...

```
SELECT ?X
WHERE{ ?X rdf:type foaf:Person
       OPTIONAL { ?X foaf:homepage ?H }
       GRAPH boundcheck.ttl {?H :is :unbound } }
```

where the aux. graph boundcheck.ttl contains the single triple [] :is :unbound.

SPARQL's formal semantics

SPARQL1.0 Formal Semantics

Graph patterns

- BGP
- $P1 . P2$
- $P \text{ FILTER } R$
- $P1 \text{ UNION } P2$
- $P1 \text{ OPTIONAL } P2$
- $\text{GRAPH } G \{ P \}$

Semantics

- $\text{eval}(P, D(G)) \dots$

P is a graph pattern

recursively defined for all graph patterns in Section 12.5 of

<http://www.w3.org/TR/rdf-sparql-query/>

D is a dataset, G is the “active graph”

Just as for RDF, the spec. semantics is a bit hard to read ...

Formal Semantics á la [Perez et al. 2006]

Easier to explain... let's steal from that here and explain the diffs:

Definition 1:

The evaluation of the BGP P over a graph G , denoted by $\text{eval}(P,G)$, is the set of all mappings $\mu: \text{Var} \rightarrow V(G)$ such that:

$\text{dom}(\mu)$ is exactly the set of variables occurring in P
 $\mu(P) \subseteq G$

Example Graph:

```
:tim          foaf:knows      :jim .
:jim          foaf:knows      :tim .
:tim          foaf:knows      :lalana .
```

Example Pattern:

$P = \{ ?X \text{ foaf:knows } ?Y \}.$

$\text{eval}(P,G) = \{ \mu1 = \{ ?x \rightarrow :tim, ?y \rightarrow :jim \}, \mu2 = \{ ?x \rightarrow :jim, ?y \rightarrow :tim \}, \mu3 = \{ ?x \rightarrow :tim, ?y \rightarrow :lalana \} \}$

Algebra á la [Perez et al. 2006]

Definition 2:

mappings μ_1, μ_2 are compatible iff they agree in their shared variables.

Let M_1, M_2 be sets of mappings

$P_1 \cdot P_2$

Definition 3:**Join:**

$$M_1 \bowtie M_2 = \{ \mu_1 \cup \mu_2 \mid \mu_1 \in M_1, \mu_2 \in M_2, \text{ and } \mu_1, \mu_2 \text{ are compatible} \}$$

$P_1 \text{ UNION } P_2$

Union:

$$M_1 \cup M_2 = \{ \mu \mid \mu \in M_1 \text{ or } \mu \in M_2 \}$$
Diff:

$$M_1 \setminus M_2 = \{ \mu \in M_1 \mid \text{forall } \mu' \in M_2, \mu \text{ and } \mu' \text{ are not compatible} \}$$

$P_1 \text{ OPTIONAL } P_2$

LeftJoin:

$$M_1 \bowtie\! \bowtie M_2 = (M_1 \bowtie M_2) \cup (M_1 \setminus M_2)$$

$P \text{ FILTER } R$

Filter:

$$M|_R = \{ \mu \mid \mu \in M \text{ and } \mu(R) = \text{true} \}$$

Semantics full as per [Perez et al.2006]

$eval(BGP, G)$... see **Definition 1**

$eval(P1 . P2, G) = eval(P1, G) \bowtie eval(P2, G)$

$eval(P1 \text{ UNION } P2, G) = eval(P1, G) \cup eval(P2, G)$

$eval(P1 \text{ OPTIONAL } P2, G) = eval(P1, G) \bowtie eval(P2, G)$

$eval(P \text{ FILTER } R, G) = eval(P, G) |_R$

As for GRAPH patterns, the extension from $eval(P, G)$ to $eval(P, D(G))$ is straightforward:

Let $D = \{G, (G_1, N_1), \dots, (G_n, N_n)\}$

- for top query patterns evaluation is equal to $eval(P, G)$,
- $eval(\text{GRAPH } N_i P, D(G)) = eval(P, G_i)$ such that (G_i, N_i) in D
- $eval(\text{GRAPH } ?Var P, D(G)) = \bigcup_{\text{for all } (G_i, N_i) \text{ in } D} eval(P, G_i) \cup \{\{?Var \rightarrow N_i\}\}$

ISSUE 1) Recall from before:
SPARQL allows duplicates !

Unions of conjunctive queries

Example:

*“Give me all names of co-authors **or** friends of Tim Berners-Lee”*

```
PREFIX foaf: <http://xmlns.com/foaf/0.1/>
SELECT ?N
WHERE {
  { [ foaf:maker <http://dblp.13s.de/.../authors/Tim_Berners-Lee>,
    [ foaf:name ?N ] ] . }
  UNION
  { <http://www.w3.org/People/Berners-Lee/card#i>
    ?F foaf:name ?N }
}
```

Note: Duplicates possible,
 bag/multiset semantics!

?N
"Lalana Kagal"
"Tim Berners-Lee"
"Dan Connolly"
"Jim Hendler"
...
"Michael Hausenblas"
"Jim Hendler"
"Charles McCathieNevile"
...

ISSUE 2) Similar troubles with duplicates from Projection & What about Blank nodes in patterns?

Example from before, but now with projection:

```
PREFIX foaf: <http://xmlns.com/foaf/0.1/>
SELECT ?X
FROM <graph>
WHERE { ?X foaf:knows [] }
```

*Blank nodes “behave” like (non-distinguished) variables in BGP*s

graph:

```
:tim          foaf:knows      :jim .
:jim          foaf:knows      :tim .
:tim          foaf:knows      :lalana .
```

?X
:tim
:jim
:tim

ISSUE 3) Recall from before:
FILTERS can make OPTIONAL non-compositional!

■ **“Conditional OPTIONAL”**

- *“Give me the names and only of those whose name starts with ‘D’ the homepage”*

```

SELECT  ?N ?H
WHERE{  ?X foaf:name ?N
        OPTIONAL { ?X foaf:homepage ?H
                    FILTER ( regex( str(?N), "^D" ) ) }
      }

```

OPTIONAL is NOT modular/compositional!
 (?N is not considered unsafe in this FILTER)*

N	H
"Lalana Kagal"	-
"Tim Berners-Lee"	-
"Dan Connolly"	-
"Daniel J. Weitzner"	< http://www.w3.org/People/Weitzner.html > 
"m. c. schraefel"	-
"Paul André"	-
"Ryen White"	-
"Desney S. Tan"	< http://research.microsoft.com/%7Edesney/ > 
"Tim Berners-Lee"	-
"Sunny Consolvo"	-

Adapting [Perez et al. 2006]

ISSUE 1) Algebra operations need to be adapted to multiset/bag semantics:

Definition 3:

Join:

$$M1 \bowtie M2 = \{ \mu1 \cup \mu2 \mid \mu1 \in M1, \mu2 \in M2, \text{ and } \mu1, \mu2 \text{ are compatible} \}$$

Union:

$$M1 \cup M2 = \{ \mu \mid \mu \in M1 \text{ or } \mu \in M2 \}$$

Diff:

$$M1 \setminus M2 = \{ \mu \in M1 \mid \text{forall } \mu' \in M2, \mu \text{ and } \mu' \text{ are not compatible} \}$$

LeftJoin:

~~$$M1 \bowtie M2 = (M1 \bowtie M2) \cup (M1 \setminus M2)$$~~

Filter:

$$M|_R = \{ \mu \mid \mu \in M \text{ and } \mu(R) = \text{true} \}$$

ISSUE 3) non-compositionality of FILTERs in OPTIONAL

Semantics as per SPARQL1.0 spec:

$$\begin{aligned}
 eval(BGP, G) & \quad \dots \text{ see Definition 1} \\
 eval(P1 . P2, G) & \quad = eval(P1, G) \bowtie eval(P2, G) \\
 eval(P1 \text{ UNION } P2, G) & \quad = eval(P1, G) \cup eval(P2, G) \\
 eval(P \text{ FILTER } R, G) & \quad = eval(P, G) \upharpoonright_R
 \end{aligned}$$

$eval(P1 \text{ OPTIONAL } \{P2 \text{ FILTER } R\}, G)$ consists of all μ such that:

1. $\mu = \mu1 \cup \mu2$, such that
 $\mu1 \in eval(P1, G)$ and $\mu2 \in eval(P2, G)$ are compatible and $\mu(R) = \text{true}$, or
2. $\mu \in eval(P1, G)$ and
there is no compatible $\mu2 \in eval(P2, G)$ for μ , or
3. $\mu \in eval(P1, G)$ and
for any compatible $\mu2 \in eval(P2, G)$, $\mu \cup \mu2$ does not satisfy R .

Addresses
ISSUE 3) non-
compositionali
ty of FILTERs
in OPTIONAL

What about Issue 2?

Definition 1:

The evaluation of the BGP P over a graph G , denoted by $\text{eval}(P,G)$, is the set of all mappings $\mu: \text{Var} \rightarrow V(G)$ such that:

$\text{dom}(\mu)$ is exactly the set of variables occurring in P

$\mu(P) \subseteq G$

Example Graph:

```
:tim          foaf:knows      :jim .
:jim          foaf:knows      :tim .
:tim          foaf:knows      :lalana .
```

Example Pattern:

$P = \{ ?X \text{ foaf:knows } ?Y \}.$

$\text{eval}(P,G) = \{ \mu_1 = \{ ?x \rightarrow :tim, ?y \rightarrow :jim \}, \mu_2 = \{ ?x \rightarrow :jim, ?y \rightarrow :tim \}, \mu_3 = \{ ?x \rightarrow :tim, ?y \rightarrow :lalana \} \}$

What about Issue 2?

Definition 1:

The evaluation of the BGP P over a graph G , denoted by $\text{eval}(P,G)$, is the set of all mappings $\mu: \text{Var} \rightarrow V(G)$ such that:

$\text{dom}(\mu)$ is exactly the set of variables occurring in P

$\mu(P) \subseteq G$

Example Graph:

```
:tim          foaf:knows      :jim .
:jim          foaf:knows      :tim .
:tim          foaf:knows      :lalana .
```

Example Pattern:

```
P = { ?X foaf:knows _ :Y } .
```

```
eval(P,G) = {}
```

What about Issue 2?

Addresses **Issue 2**) We mean here the multiset wrt to the number of existing instance mappings wrt. Simple Entailment

Definition 1:

The evaluation of the BGP P over a graph G , denoted by $\text{eval}(P,G)$, is the **multiset** of all mappings $\mu: \text{Var} \rightarrow V(G)$ such that:

$\text{dom}(\mu)$ is exactly the set of variables occurring in P

$\mu(P) \models G$

Example Graph:

```
:tim          foaf:knows      :jim .
:jim          foaf:knows      :tim .
:tim          foaf:knows      :lalana .
```

Example Pattern:

```
P = { ?X foaf:knows _ :Y }.
```

```
eval(P,G) = { { μ1 = { ?x → :tim }, μ2 = { ?x → :jim },
               μ3 = { ?x → :tim } } }
```

Some academic works around SPARQL1.0

SPARQL semantics

- [Perez et al. 2006] (pre-dates the spec) [Perez et al. 2009]

SPARQL equivalences

- also in [Perez et al. 2006],[Perez et al. 2009]
- More in [Schmidt et al. 2010]

SPARQL expressivity

- Reducible to datalog with negation [Polleres 2007]
- Other way around also works [Angles & Gutierrez 2008]

Proposed Extensions

- Property Paths [Alkhateeb et al. 2009], [Perez et al. 2008]
- Aggregates [Polleres et al. 2007]

Another example from DBPedia (time allowed...)

Conjunction (.) , disjunction (UNION), optional (OPTIONAL) patterns and filters (FILTER)

Cities in Finland with optionally their German (@de) name

```
SELECT ?C ?N
WHERE
{
  ?C dct:subject category:Cities_and_towns_in_Finland .
  OPTIONAL { ?C rdfs:label ?N . FILTER( LANG(?N) = "de" ) }
}
```

C	N
http://dbpedia.org/resource/Hanko	"Hanko"@de
http://dbpedia.org/resource/Espoo	"Espoo"@de
http://dbpedia.org/resource/Lohja	"Lohja"@de
http://dbpedia.org/resource/Kotka	"Kotka"@de
http://dbpedia.org/resource/Hyvink%C3%A4	
http://dbpedia.org/resource/Lahti	"Lahti"@de
http://dbpedia.org/resource/Akaa	"Akaa"@de
http://dbpedia.org/resource/Pori	"Pori"@de
http://dbpedia.org/resource/Raah	"Raahelä"@de
http://dbpedia.org/resource/Oulu	"Oulu"@de
http://dbpedia.org/resource/Kemi	"Kemi"@de
http://dbpedia.org/resource/Turku	"Turku"@de
http://dbpedia.org/resource/Rauma,_Finland	"Rauma"@de
http://dbpedia.org/resource/Vaasa	"Vaasa"@de
http://dbpedia.org/resource/Helsingfors	
http://dbpedia.org/resource/Nokia,_Finland	"Nokia (Stadt)"@de
http://dbpedia.org/resource/Ule%C3%A5borg	

BTW, why does “Helsingfors” not have a German label?



Helsingfors is the Swedish name of Helsinki, and only exists in dbpedia as a redirect to Helsinki:

property	hasValue	isValueOf
owl:sameAs	-	http://www4.wiwiss.fu-berlin.de/flickrwrappr/photos/Helsingfors
dbpedia:ontology/deathPlace	-	:Ossian_Schauman
dbpedia:ontology/birthPlace	-	:Lydia_Chukovskaya
dbpedia:ontology/birthPlace	-	:Olav_Ri%C3%A9go
foaf:primaryTopic	-	http://en.wikipedia.org/wiki/Helsingfors
rdfs:label	"Helsingfors"@en	-
dbpedia:ontology/wikiPageRedirects	:Helsinki	-
http://purl.org/dc/terms/subject	:Category:Cities_and_towns_in_Finland	-
foaf:page	http://en.wikipedia.org/wiki/Helsingfors	-

We can use the IF-THEN-ELSE feature of **OPTIONAL** to fix this query, can't we?

SIEMENS

Cites Finland with optionally (if they have one) their German (@de) name ... and otherwise try to find whether there is a redirect to a resource with a German name

```
SELECT ?C ?N
WHERE
{
  ?C dcterms:subject category:Cities_and_towns_in_Finland .
  OPTIONAL { ?C rdfs:label ?N . FILTER( LANG(?N) = "de" ) }
  OPTIONAL { ?C dbont:wikiPageRedirects [rdfs:label ?N] . FILTER( LANG(?N) = "de" ) }
}
```

Unfortunately doesn't work as intended on DBpedia SPARQL endpoint, cf.

<https://twitter.com/#!/AxelPolleres/status/189257251154960384>

Assignments/Final project:

Assignment 3:

- Some more SPARQL queries, to be published on the lecture homepage this week, to be solved by next lecture.

Final projects:

- Could be some application where you do something interesting with Linked Data
- Could be presenting a tool or system that uses Semantic Web technologies.
- Can be done in groups of 2.
- You have to send me a proposal (by next lecture), what you plan to present which credibly argues that
 - a) it is interesting
 - b) your overall effort is around 20hrs/person (incl. presentation preparation)
- Alternatively: I will think of some topics (typically, summarizing 2-3 papers you have to read and present them), will be presented next time or you can make some suggestions per mail.

References

- [Perez et al. 2006] Jorge Pérez, [Marcelo Arenas](#), [Claudio Gutierrez](#): Semantics and Complexity of SPARQL. [International Semantic Web Conference 2006](#): 30-43
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- [Polleres 2007] Axel Polleres: From SPARQL to rules (and back). [WWW 2007](#): 787-796
- [Angles & Gutierrez 2008] Renzo Angles, [Claudio Gutierrez](#): The Expressive Power of SPARQL. [International Semantic Web Conference 2008](#): 114-129
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